





#### Models with constant load

- (ii) 'outward variant': increase of fragility depends on *out-degree* 
  - ▶ load of failing node (i.e. 1) is shared equally among neighbors

$$\phi_i(t) = \sum_{j \in \mathrm{nb}_{\mathrm{in}}(i,\mathcal{A})} \frac{s_j(t)}{k_j^{\mathrm{out}}}$$

- undirected, regular networks:
  - inward and outward variant equivalent
- heterogeneous degree:
  - ▶ failing high-degree nodes cause *less* damage then low-degree nodes
- high-degree node:
  - high vulnerability if connected to low-degree nodes (dissortative networks)

# Models with load redistribution

#### • assumptions:

- 'load' is represented by fragility  $\phi_i$
- failed nodes distribute total fragility
- changes in fragility  $\phi_i$  do depend on  $\phi_j$
- examples:
  - ▶ (FBM) fiber bundle model (Kun et. al, 2000)
  - cascading models in power grids (Kinney et. al, 2005)
- variants:
  - ► LLSC: total load is conserved (FBM), local load is shared if nodes fail, links remain active ⇒ broad redistribution
  - ► LLSS: local load shedding: if nodes fail, links break ⇒ fragmented network
- does 'globalization' increases systemic risk?
  - network allows to redistribute load (risk), but also to receive load (risk) from far distant nodes



- ▶ replace  $\phi_i \rightarrow (\phi_i \theta_i)$
- result:
  - much smaller cascades (compared to ii)
  - high initial overload needed to trigger cascades

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J. Lorenz, S. Battiston, F. Schweitzer: Systemic Risk in a Unifying Framework for Cascading Processes on Networks, *European Physical Journal B* vol 71, no 4 (2009) pp. 441-460, http://arxiv.org/abs/0907.5325

•  $\langle \theta \rangle_{X(t)}$ : normalized first moment of  $\theta$  below X-quantile of  $p_{\theta}$ 

• recursive dynamics with fix point  $X^{\star}$ 

 $X(t+1) = P_{\theta}(\langle \phi(t) \rangle)$ 

15 / 36

16 / 36



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- Costs of banking crisis (wave of bank defaults) are high for economy – measured in output loss of GDP\*
- $\bullet\,$  taking systemic risk can enhance overall growth despite of occasional severe crisis^{\dagger}\,



 $^{*}$  Hoggarth, G.; Reis, R. & Saporta, V. Costs of banking system instability: Some empirical evidence Journal of Banking and Finance 2002

<sup>T</sup>Ranciere, R.; Tornell, A. & Westermann, F. *Systemic Crises and Growth* Quarterly Journal of Economics, 2008

 $+\alpha \operatorname{sign}(\Delta \phi(t))$ 

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| Trend Reinforcing   |                  |   |                     |         |
|   |                  |   |                     |         |

 $\sigma\xi(t)$ 

# **Trend Reinforcement Model**

• Fragility of *n* firms evolves as

 $\phi(t+1) = \phi(t) +$ 

- fragility stochastic shocks trend reinforcing
- trend reinforcing  $\nearrow \rightsquigarrow \nearrow \nearrow$ ,
- $\bullet$  reducing volatility  $\sigma$ 
  - ► decreases stochastic shocks → less bankruptcies, BUT
  - ► reduces possibility to break bad trends → more bankrupcies!
- <u>Conclusion</u>: We are safest with intermediate volatility



 $\alpha = 0.05$   $\sigma = 0.2$  21 bankrupto

<sup>T</sup>Lorenz, Jan, Battiston, Stefano: Systemic risk in a network fragility model analyzed with probability density evolution of persistent random walks , Networks and Heterogeneous Media, vol. 3, no. 2, June (2008), pp. 185-200

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#### Local optimum explained by stochastic process

• Scaling of displacement for Gaussian Random Walk (GRW) and Persistent Random Walk (PRW)



<sup>T</sup>Lorenz, Jan, Battiston, Stefano: Systemic risk in a network fragility model analyzed with probability density evolution of persistent random walks , Networks and Heterogeneous Media, vol. 3, no. 2, June (2008), pp. 185-200

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# Conclusions

- general framework for systemic risk
  - **microlevel:** interplay between fragility  $(\phi_i)$  and threshold  $(\theta_i)$
  - macrolevel: fraction of failed nodes,  $X(t) \Rightarrow$  prediction
- different model classes with unique behavior
  - ▶ (i) constant load, (ii) load redistribution, (iii) overload redistribution
  - phase transition: small changes lead to big impact in systemic risk
  - systemic risk increases for medium heterogeneity
- mechanisms of systemic risk
  - contagion: donations, voter model, social activation,
  - load redistribution: additional reinforcement
  - trend reinforcement: bankrupcies can increase
- role of stochasticity
  - optimal volatility to break bad trends

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